

# Function Analysis Part 1 Assignment

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## Function Analysis Part 1 Assignment

### Question 0

Watch the lecture video [here](#).

Did you watch the video? [Type yes or no.]

Analyze the following functions using the steps from class.

### Question 1

$$f(x) = \frac{9x - 1}{\frac{1}{5}x^2 + 22}$$

[We'll work through this one together in class. Look out for the three inflection points - they may not be obvious on our first graph.]

Step 1: Find the domain of  $f$ .

1

Step 2: Find the derivative  $f'$ .

2

Step 3: Find the critical points of  $f$  (where  $f'$  is 0 or undefined).

3

Step 4: See if the sign of  $f'$  actually changes at the critical points of  $f$ , and determine whether  $f$  has a local maximum or local minimum at these points.

4

Step 5: Find the second derivative  $f''$ .

5

Step 6: Find the critical points of  $f'$  (where  $f''$  is 0 or undefined).

6

Step 7: See if the sign of  $f''$  actually changes at the critical points of  $f'$ , and determine whether  $f$  has an inflection point at these points.

7

Step 8: Find the  $x$ - and  $y$ -intercepts.

8

Step 9: Determine the end behavior.

9

Step 10: Make an informed graph. Mark any  $x$ - and  $y$ -intercepts, relative maxima and minima, and inflection points.

10

Step 11: Discuss absolute max/min, increasing/decreasing, concave up/down.

## Question 2

$$g(x) = 2x^4 - 8x^3 - x^2 + 30x$$

[Caution:  $g$  has two x-intercepts. When you solve  $g(x) = 0$ , Sage will give you four answers, but only two are real. Convert to decimals and watch out for scientific notation.]

Step 1: Find the domain of  $g$ .

11

Step 2: Find the derivative  $g'$ .

12

Step 3: Find the critical points of  $g$  (where  $g'$  is 0 or undefined).

13

Step 4: See if the sign of  $g'$  actually changes at the critical points of  $g$ , and determine whether  $g$  has a local maximum or local minimum at these points.

14

Step 5: Find the second derivative  $g''$ .

15

Step 6: Find the critical points of  $g'$  (where  $g''$  is 0 or undefined).

16

Step 7: See if the sign of  $g''$  actually changes at the critical points of  $g'$ , and determine whether  $g$  has an inflection point at these points.

17

Step 8: Find the  $x$ - and  $y$ -intercepts.

18

Step 9: Determine the end behavior.

19

Step 10: Make an informed graph. Mark any  $x$ - and  $y$ -intercepts, relative maxima and minima, and inflection points.

20

Step 11: Discuss absolute max/min, increasing/decreasing, concave up/down.