Examples of embedding Sage in $I\!\!A T_E\!X$ with ${\sf SageT}_E\!X$

Drake and others

March 9, 2019

1 Inline SageMath, code blocks

This is an example 2 + 2 = 4. If you raise the current year mod 100 (which equals 18) to the power of the current day (9), you get 324. Also, 2019 modulo 42 is 2.

Code block, which uses a variable \mathbf{s} to store the solutions:

1+1 var('a,b,c,d') eqn = [a+b*c==1, b-a*c==0, a+b==5] s = solve(eqn, a,b,c)

Solutions of eqn = [bc + a = 1, -ac + b = 0, a + b = 5]:

$$\begin{bmatrix} a = -\frac{1}{4}i\sqrt{79} + \frac{11}{4}, b = \frac{1}{4}i\sqrt{79} + \frac{9}{4}, c = \frac{1}{10}i\sqrt{79} + \frac{1}{10} \end{bmatrix}$$
$$\begin{bmatrix} a = \frac{1}{4}i\sqrt{79} + \frac{11}{4}, b = -\frac{1}{4}i\sqrt{79} + \frac{9}{4}, c = -\frac{1}{10}i\sqrt{79} + \frac{1}{10} \end{bmatrix}$$

Now we evaluate the following block:

E = EllipticCurve("37a")

You can't do assignment inside **\sage** macros, since Sage doesn't know how to typeset the output of such a thing. So you have to use a code block. The elliptic curve E given by $y^2 + y = x^3 - x$ has discriminant 37.

You can do anything in a code block that you can do in Sage and/or Python. Here we save an elliptic curve into a file.

```
try:
    E = load('E2')
except IOError:
    E = EllipticCurve([1,2,7,4,5])
    E.anlist(100000)
    E.save('E2')
```

The 9999th Fourier coefficient of $y^2 + xy + 3y = x^3 + 2x^2 + 4x + 5$ is -27. The following code block doesn't appear in the typeset file... but we can refer to whatever we did in that code block: e = 7.

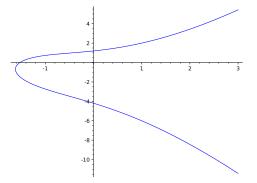
$$var('x')$$

f(x) = log(sin(x)/x)

The Taylor Series of f begins: $x \mapsto -\frac{1}{467775} x^{10} - \frac{1}{37800} x^8 - \frac{1}{2835} x^6 - \frac{1}{180} x^4 - \frac{1}{6} x^2$.

2 Plotting

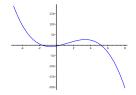
Here's a plot of the elliptic curve E.



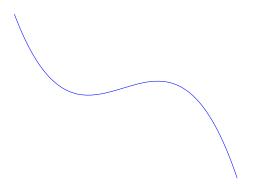
You can use variables to hold plot objects and do stuff with them.

$$p = plot(f, x, -5, 8)$$

Here's a small plot of f from -5 to 5, which I've centered:



On second thought, use the default size of 3/4 the **\textwidth** and don't use axes:

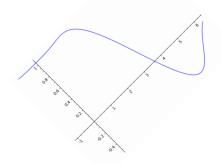


Remember, you're using Sage, and can therefore call upon any of the software packages Sage is built out of.

f = maxima('sin(.4 * x)^3*cos(x)')
g = f.integrate('x')

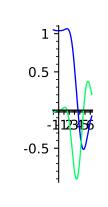
Plot g(x), but don't typeset it.

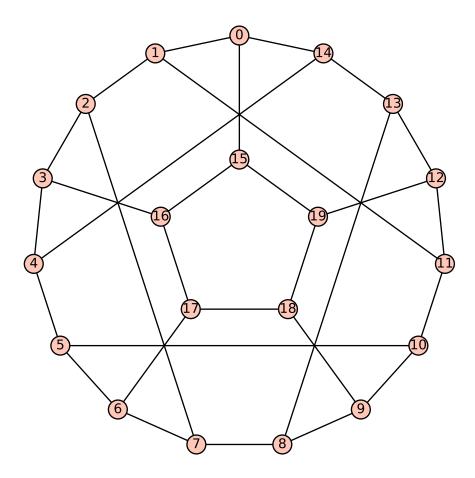
You can specify a file format and options for includegraphics. The default is for EPS and PDF files, which are the best choice in almost all situations. (Although see the section on 3D plotting.)



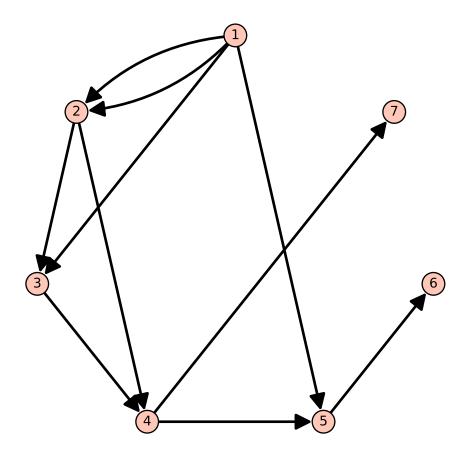
If you use regular latex to make a DVI file, you'll see a box, because DVI files can't include PNG files. If you use pdflatex that will work. See the documentation for details.

When using \sageplot, you can pass in just about anything that Sage can call .save() on to produce a graphics file:





G4 = DiGraph({1:[2,2,3,5], 2:[3,4], 3:[4], 4:[5,7], 5:[6]},\
multiedges=True)
G4plot = G4.plot(layout='circular')



Indentation and so on works fine.

```
s = 7
s2 = 2^s
P.<x> = GF(2)[]
M = matrix(parent(x),s2)
for i in range(s2):
```

```
p = (1+x)^i
pc = p.coeffs()
a = pc.count(1)
for j in range(a):
    idx = pc.index(1)
    M[i,idx+j] = pc.pop(idx)
```

```
matrixprogram = matrix_plot(M,cmap='Greys')
```

And here's the picture:

??

Reset \mathbf{x} in Sage so that it's not a generator for the polynomial ring: \mathbf{x}

2.1 3D plotting

3D plotting right now is problematic because there's no convenient way to produce vector graphics. We can make PNGs, though, and since the **sageplot** command defaults to EPS and PDF, *you must specify a valid format for 3D plotting.* Sage right now (version 3.4.2) can't produce EPS or PDF files from plot3d objects, so if you don't specify a valid format, things will go badly. You can specify the "imagemagick" option, which will use the Imagemagick convert utility to make EPS files. See the documentation for details.

Here's the famous Sage cube graph:

```
G = graphs.CubeGraph(5)
```

```
??
```

3 Pausing SageT_EX

Sometimes you want to "pause" for a bit while writing your document if you have embedded a long calculation or just want to concentrate on the IATEX and ignore any Sage stuff. You can use the <code>\sagetexpause</code> and <code>\sagetexunpause</code> macros to do that.

A calculation: (SageT_EX is paused) and a code environment that simulates a time-consuming calculation. While paused, this will get skipped over.

```
import time
time.sleep(15)
```

Graphics are also skipped:

 $SageT_EX$ is paused; no graphic

4 Make Sage write your LATEX for you

With SageTEX, you can not only have Sage do your math for you, it can write parts of your LATEX document for you! For example, I hate writing tabular environments; there's too many fiddly little bits of punctuation and whatnot... and what if you want to add a column? It's a pain—or rather, it was a pain. Here's how to make Pascal's triangle. It requires the amsmath package because of what Sage does when producing a LATEX representation of a string. (It puts it inside a \text macro.)

Okay, now here's the table. To change the size, edit n above. If you have several tables, you can use this to get them all the same size, while changing only one thing.

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